Once a user is logged into the chat room, their name appears in the user list on the right side of the chat window (if you've got the user list active).

Any user can invite any other user into a private chat by clicking on the user name, and then selecting the Private Chat prompt.